

# Chapter 3 Exponential and Logarithmic Functions

Course Number

Instructor

Date

## Section 3.1 Exponential Functions and Their Graphs

**Objective:** In this lesson you learned how to recognize, evaluate, and graph exponential functions.

### Important Vocabulary

Define each term or concept.

**Algebraic functions**

**Transcendental functions**

**Natural base  $e$**

**Continuous compounding**

### I. Exponential Functions (Page 218)

The **exponential function  $f$  with base  $a$**  is denoted by \_\_\_\_\_, where  $a > 0$ ,  $a \neq 1$ , and  $x$  is any real number.

#### *What you should learn*

How to recognize and evaluate exponential functions with base  $a$

**Example 1:** Use a calculator to evaluate the expression  $5^{3/5}$ .

### II. Graphs of Exponential Functions (Pages 219–221)

For  $a > 1$ , is the graph of  $y = a^x$  increasing or decreasing over its domain? \_\_\_\_\_

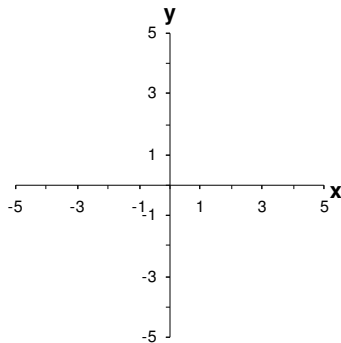
For  $a > 1$ , is the graph of  $y = a^{-x}$  increasing or decreasing over its domain? \_\_\_\_\_

For the graph of  $y = a^x$  or  $y = a^{-x}$ ,  $a > 1$ , the domain is \_\_\_\_\_, the range is \_\_\_\_\_, and the intercept is \_\_\_\_\_. Also, both graphs have \_\_\_\_\_ as a horizontal asymptote.

#### *What you should learn*

How to graph exponential functions and use the One-to-One Property

**Example 2:** Sketch the graph of the function  $f(x) = 3^{-x}$ .



The graph of the exponential function passes the \_\_\_\_\_ Test, and therefore, the function is a one-to-one function (and, thus, has an inverse function).

State the One-to-One Property for exponential functions and explain how it may be used to solve simple exponential equations.

### III. The Natural Base $e$ (Page 222)

The **natural exponential function** is given by the function \_\_\_\_\_. In this function, \_\_\_\_\_ is the constant and \_\_\_\_\_ is the variable.

***What you should learn***

How to recognize, evaluate, and graph exponential functions with base  $e$

**Example 3:** Use a calculator to evaluate the expression  $e^{3/5}$ .

**IV. Applications of Exponential Functions** (Pages 223–225)

After  $t$  years, the balance  $A$  in an account with principal  $P$  and annual interest rate  $r$  (in decimal form) is given by the formulas:

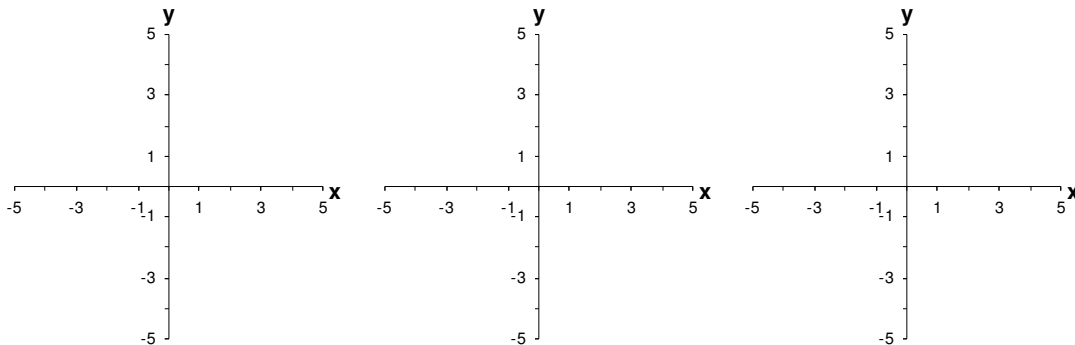
For  $n$  compoundings per year: \_\_\_\_\_

For continuous compounding: \_\_\_\_\_

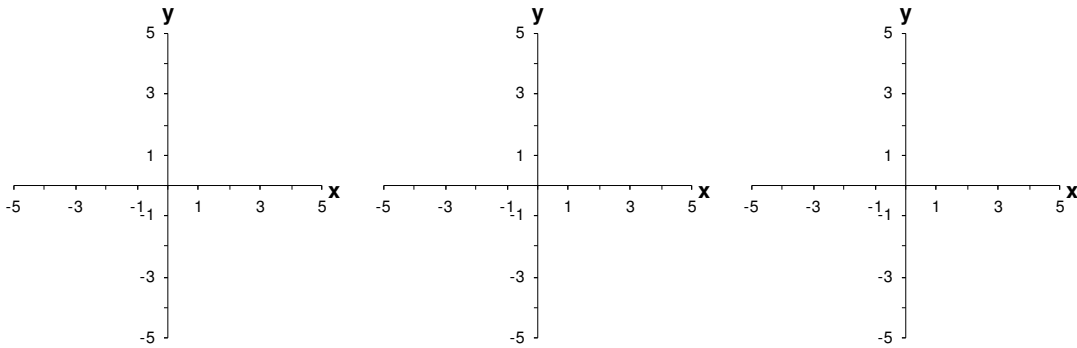
*What you should learn*  
 How to use exponential functions to model and solve real-life applications

- Example 4:** Find the amount in an account after 10 years if \$6000 is invested at an interest rate of 7%,
- (a) compounded monthly.
  - (b) compounded continuously.

**Additional notes**



Additional notes



**Homework Assignment**

Page(s)

Exercises